

# Microwave dielectric properties of $(1-x)\text{CeO}_2-x\text{CaTiO}_3$ and $(1-x)\text{CeO}_2-x\text{Sm}_2\text{O}_3$ ceramics

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## Abstract

$\text{CeO}_2\text{-CaTiO}_3$  and  $\text{CeO}_2\text{-Sm}_2\text{O}_3$  microwave dielectric ceramics have been prepared by a conventional solid state ceramic route. The dielectric ceramics are characterized by X-ray diffraction, SEM, Raman and microwave methods. Ceria has a relative dielectric constant,  $\epsilon_r$ , of 23, high dielectric quality factor  $\times$  frequency product,  $Q \times f$  up to 60,000 GHz with high temperature coefficient of resonant frequency,  $\tau_f$ , of  $-53$  ppm/ $^\circ\text{C}$ . The addition of  $\text{CaTiO}_3$  and samarium oxide leads to a zero temperature variation of resonant frequency. The relative dielectric constant increases and  $Q$  decrease with  $\text{CaTiO}_3$  addition and the  $\tau_f$  changes from a negative to a positive value.  $\text{Sm}_2\text{O}_3$  addition of up to 50 mol% increases  $Q$ , decreases  $\epsilon_r$  and improves the  $\tau_f$ . The microwave dielectric properties are measured at low temperatures down to 20 K. The effect of addition of 1 mol% of various rare earth oxides on the microwave dielectric properties of ceria has also been investigated.

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**Keywords:**  $\text{CeO}_2$ ;  $\text{Sm}_2\text{O}_3$ ;  $\text{CaTiO}_3$ ; Microwave ceramics; Dielectric resonators

## 1. Introduction

Several research groups have developed microwave dielectric resonators (DRs) with satisfactory dielectric properties.<sup>1</sup> Ceramic materials for DR applications should have high quality factor ( $Q$ ), high relative permittivity ( $\epsilon_r$ ) and the stability of these parameters in the working temperature and frequency ranges. Ceria-based materials have been intensively investigated as catalysts, structural and electronic promoters of heterogeneous catalytic reactions and oxide ion conducting solid electrolytes in electrochemical cells.<sup>2</sup> Recently we showed ceria to be a good dielectric resonator material with a  $\epsilon_r = 23$ , quality factor ( $Q \times f$ ) of about 60,000. We also demonstrated that the addition of 1 mol%  $\text{CaCO}_3$  increases the  $Q$ .<sup>3</sup> But the temperature coefficient of resonant frequency ( $\tau_f$ ) of ceria has a large negative value ( $-53$  ppm/ $^\circ\text{C}$ ), which precludes its use in practical applications. It is possible to achieve temperature com-

penensation by preparing a solid solution phase between compounds having positive and negative  $\tau_f$  values.<sup>4–8</sup> The perovskite  $\text{CaTiO}_3$  has<sup>9</sup> a high positive value of  $\tau_f$  (800 ppm/ $^\circ\text{C}$ ). In the present work we report the microwave dielectric properties of ceria with different amounts of additives such as  $\text{CaTiO}_3$  and  $\text{Sm}_2\text{O}_3$  which exhibit a positive values of  $\tau_f$ . The effect of various rare earth oxides on the microwave dielectric properties of ceria has also been investigated.

## 2. Experimental

The dielectric samples were prepared by a conventional solid-state ceramic route.  $\text{CeO}_2$ ,  $\text{Sm}_2\text{O}_3$ ,  $\text{CaCO}_3$ , and  $\text{TiO}_2$  with purity  $>99.9\%$  were used as starting materials. Cerium oxide and  $\text{Sm}_2\text{O}_3$  were calcined at  $800$   $^\circ\text{C}$  for 3 h to remove volatile impurities. The powders were weighed according to the compositions  $(1-x)\text{CeO}_2-x\text{Sm}_2\text{O}_3$  ( $x = 0.005, 0.01, 0.10, 0.30, 0.50, 0.70, 0.80, 0.90$  and  $0.95$ ) and  $(1-x)\text{CeO}_2-x\text{CaTiO}_3$  ( $x = 0.01, 0.02, 0.04, 0.06, 0.08, 0.10$ ) and mixed in an agate mortar using distilled water and then dried.

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The mixed powder was calcined at 1200 °C for 4 h. In the CeO<sub>2</sub>–Sm<sub>2</sub>O<sub>3</sub> system, the samples with higher contents of Sm<sub>2</sub>O<sub>3</sub> decomposed or become fine powder on aging. To avoid this, 0.5 wt.% CuO was added to the calcined powder for  $x=0.90$  and 0.95. A 5% PVA solution was added to the powder as a binder and the slurry was dried. The resulting powders were again ground well and then uniaxially pressed into pellets 14 mm in diameter and about 7 mm in height. These pellets were sintered at 1600–1650 °C for 4 h. The preferred sintering temperatures were chosen to be the temperature resulting in the highest sample density. Samples of ceria with 1 mol% of dopant (Nd<sub>2</sub>O<sub>3</sub>, Sm<sub>2</sub>O<sub>3</sub>, Eu<sub>2</sub>O<sub>3</sub>, Gd<sub>2</sub>O<sub>3</sub> and Er<sub>2</sub>O<sub>3</sub>) were also prepared as described above.

Powder X-ray diffraction (XRD) patterns of (1– $x$ )CeO<sub>2</sub>– $x$ Sm<sub>2</sub>O<sub>3</sub> and (1– $x$ )CeO<sub>2</sub>– $x$ CaTiO<sub>3</sub> were taken using CuK<sub>α</sub> radiation as a function of composition to investigate the crystalline structure. The density of the ceramic pucks was determined by the Archimedes method. Scanning electron micrographs were recorded from thermally etched samples using Hitachi SEM model No. S-4300.

Dielectric properties at microwave frequencies were measured in the 4–6 GHz frequency range. The end-shorted method proposed by Hakki and Coleman<sup>10</sup> and later modified by Courtney<sup>11</sup> was employed for the evaluation of the relative dielectric constant using the TE<sub>011</sub> mode. The dielectric quality factor of the samples was measured by the cavity method<sup>12</sup> using the TE<sub>018</sub> resonant mode. The temperature coefficient of resonant frequency was measured by noting the response of the TE<sub>011</sub> mode with respect to temperature using the Hakki and Coleman method in the 20–80 °C region. The low temperature microwave dielectric properties were measured by placing the cavity on the cold head of a closed cycle Gifford McMahon cryostat (“work-horse”, Cryophysics, Abingdon, UK) and the microwave dielectric properties were determined using a vector network analyzer (HP8720C) in the temperature range 20–300 K. The Raman spectra from the sintered pucks were recorded using a Renishaw system 2000 microprobe with a 488 nm line of an Ar<sup>+</sup> laser as exciting radiation with nominally <4.0 mW power incident on the sample surface. The laser line was focused onto the sample by a cylindrical microscope lens of ×50 magnification with a spot diameter of 3±1 μm.

### 3. Results and discussion

#### 3.1. (1– $x$ )CeO<sub>2</sub>– $x$ CaTiO<sub>3</sub> (0.1≤ $x$ ≤0) ceramics

Pure CeO<sub>2</sub> has a cubic fluorite type of structure with space group Fm3m and has a density of 7.215 g cm<sup>−3</sup>

(JCPDS file no. 43-1002). It has  $\epsilon_r=23$ ,  $Q \times f > 60,000$  (at 6 GHz) and  $\tau_f = -53$  ppm/°C.<sup>3</sup>

Fig. 1 shows the X-ray diffraction patterns recorded from (1– $x$ )CeO<sub>2</sub>– $x$ CaTiO<sub>3</sub> indicating the single phase nature of the ceramics. Fig. 2a shows the scanning electron micrograph recorded from pure CeO<sub>2</sub> and Fig. 2b 0.9CeO<sub>2</sub>–0.1CaTiO<sub>3</sub> ceramic. Pure ceria grains are large in size 20–25 μm where as the 0.9CeO<sub>2</sub>–0.1CaTiO<sub>3</sub> ceramic the grains are about 10 μm in size although both sintered at the same temperature. The SEM picture also shows the single phase nature of the ceramics.

The Raman spectra of CaTiO<sub>3</sub>-doped CeO<sub>2</sub> were measured for composites  $x < 0.06$  and given in Fig. 3. Pure CeO<sub>2</sub> has a Raman active mode (F<sub>2g</sub>) at 465 cm<sup>−1</sup> which is attributed to the symmetrical stretching mode of the Ce–O8 vibration making this mode suitable for detecting oxygen disorder. An increased addition of CaTiO<sub>3</sub> caused only a minor shift of the 465 cm<sup>−1</sup> mode from 465.6 to 465.3 cm<sup>−1</sup> and an increase in the line-width (FWHM) from 10.6 to 12.1 cm<sup>−1</sup>. The formed single phase is preceded by substitution of Ce<sup>4+</sup> in the lattice by Ti<sup>4+</sup> and Ca<sup>2+</sup> where it has been suggested in earlier FTIR study<sup>3</sup> that Ti addition decreases anharmonicity in the lattice by decreasing multiphonon absorption and Ca increases anharmonicity.

The sintered densities of the specimens, relative to the CaTiO<sub>3</sub> content are plotted in Fig. 4. The density increases with a small addition of CaTiO<sub>3</sub> ( $x=0.02$ ), but with further addition of CaTiO<sub>3</sub>, it decreases.

Fig. 5 shows the relationship between the  $\epsilon_r$  and the composition ( $x$ ) compared with those obtained by the logarithmic mixing rule  $\ln \epsilon_r = V_1 \ln \epsilon_{r1} + V_2 \ln \epsilon_{r2}$  where  $V_1$  and  $V_2$  are volume fractions of each component,  $\epsilon_{r1}$  and  $\epsilon_{r2}$  are their relative dielectric constant and  $\epsilon_r$  is the

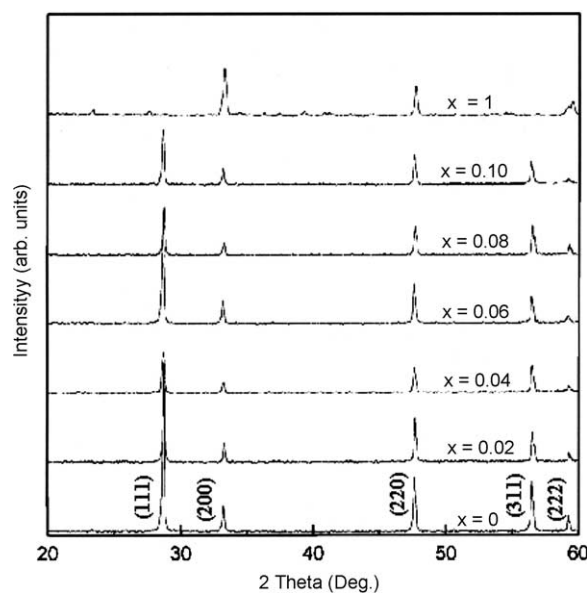


Fig. 1. Powder X-ray diffraction patterns of (1– $x$ )CeO<sub>2</sub>– $x$ CaTiO<sub>3</sub> ceramics.

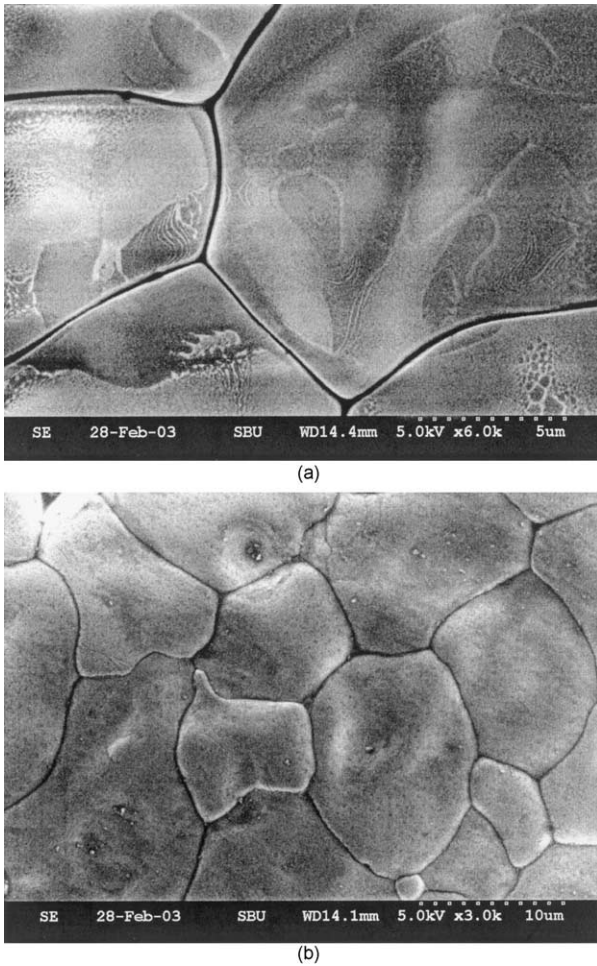


Fig. 2. Scanning electron micrographs recorded from thermally etched samples: (a)  $\text{CeO}_2 \times 6000$ ; (b)  $0.9\text{CeO}_2-0.1\text{CaTiO}_3 \times 3000$ .

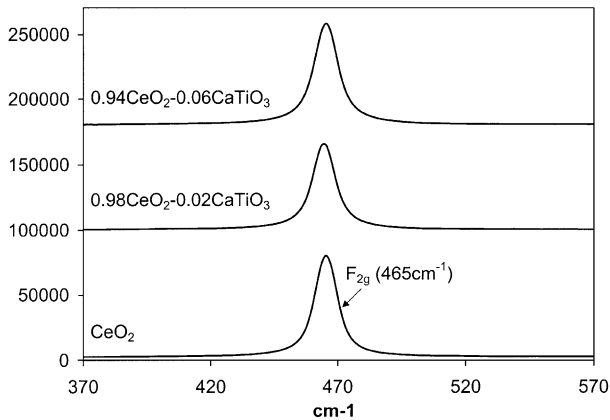


Fig. 3. Raman spectra of  $(1-x)\text{CeO}_2-x\text{CaTiO}_3$  ceramics for different values of  $x$ .

resultant relative dielectric constant of the mixture.<sup>13</sup> The  $\epsilon_r$  increases with the increasing  $\text{CaTiO}_3$  content. This is expected since  $\text{CaTiO}_3$  has a high  $\epsilon_r$  of 170.<sup>9</sup> Fig. 5 shows that the measured  $\epsilon_r$  is slightly higher than those calculated by the mixture rule. Fig. 4 shows the

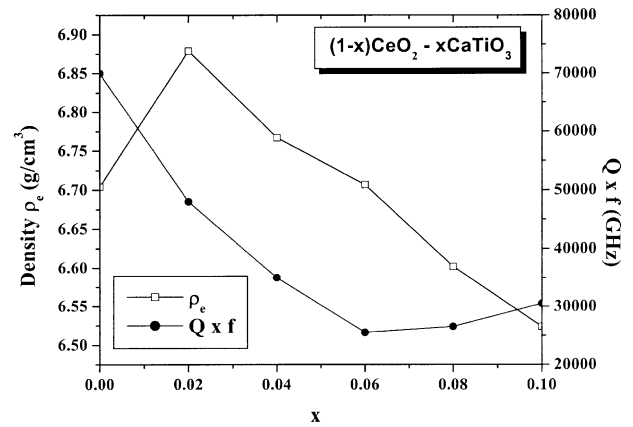


Fig. 4. The variation of experimental density and  $Q \times f$  of  $(1-x)\text{CeO}_2-x\text{CaTiO}_3$  ceramics as a function of  $\text{CaTiO}_3$  content.

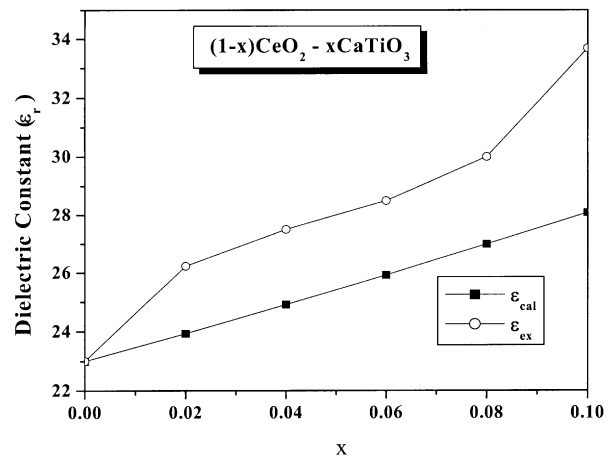


Fig. 5. Variation of experimental and calculated  $\epsilon_r$  using the mixture rule with composition in the  $(1-x)\text{CeO}_2-x\text{CaTiO}_3$  system.

effect of  $\text{CaTiO}_3$  addition on the quality factor ( $Q \times f$ ). The quality factor decreases with  $\text{CaTiO}_3$  addition. Fig. 6 shows the quality factor ( $Q \times f$ ) of  $\text{CeO}_2-\text{CaTiO}_3$  measured at low temperatures in the range 20–300 K. The increase in the quality factor is rather small on cooling until 130 K. Further cooling increases the  $Q$  considerably but much less when compared with pure ceria.

Fig. 7 shows the variation of  $\tau_f$  with composition in  $(1-x)\text{CaTiO}_3-x\text{CeO}_2$  ( $0.9 \leq x \leq 1$ ) ceramics. The  $\tau_f$  varies from  $-53$  to  $+60$  ppm/ $^\circ\text{C}$  as  $x$  varies from 0 to 0.1. The temperature compensation (zero  $\tau_f$ ) occurs at  $x = 0.057$ .

### 3.2. $(1-x)\text{CeO}_2-x\text{Sm}_2\text{O}_3$ ceramics

$\text{Sm}_2\text{O}_3$  has two phases; monoclinic with density  $7.746$   $\text{g cm}^{-3}$  [JCPDS File No. 42-1464] and cubic with density  $7.103$   $\text{g cm}^{-3}$  [JCPDS File No.15-813]. The XRD pattern recorded from crushed powders from sintered compacts of  $(1-x)\text{CeO}_2-x\text{Sm}_2\text{O}_3$  ( $0 \leq x \leq 1$ ) ceramics are shown

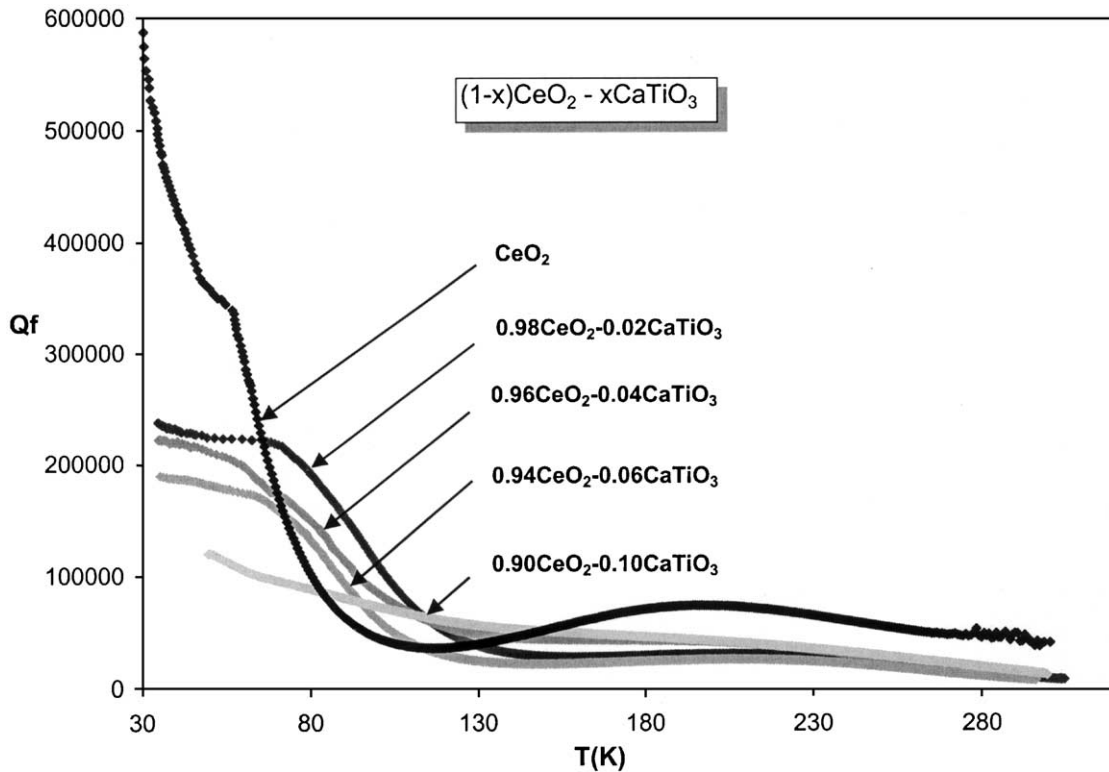


Fig. 6. Variation of quality factor ( $Q \times f$  GHz) of  $(1-x)\text{CeO}_2-x\text{CaTiO}_3$  ceramics as a function of temperature.

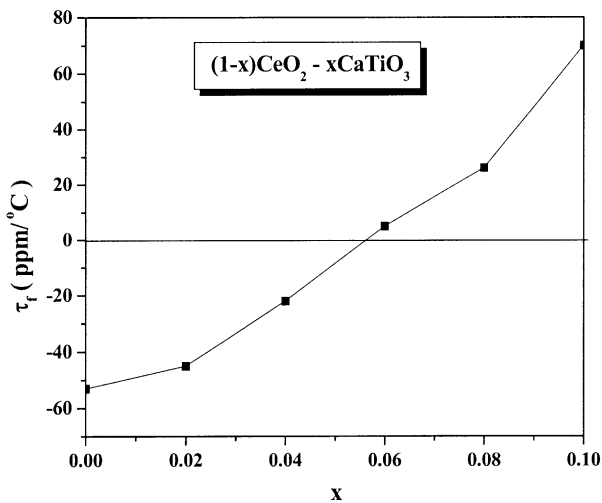


Fig. 7. Temperature coefficient of resonant frequency ( $\tau_r$ ) of  $(1-x)\text{CeO}_2-x\text{CaTiO}_3$  ceramics as a function of composition  $x$ .

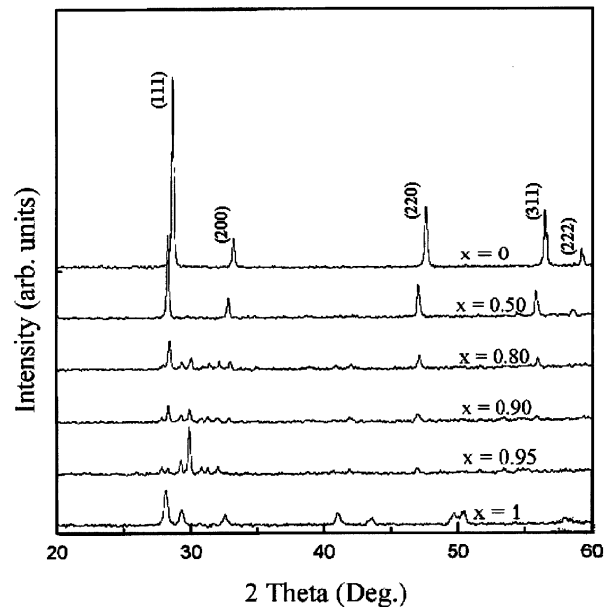


Fig. 8. The powder X-ray diffraction patterns of  $(1-x)\text{CeO}_2-x\text{Sm}_2\text{O}_3$  ceramics.

in Fig. 8. The compositions with  $x=0-0.5$  showed a cubic fluorite structure as evidenced by the XRD in Fig. 8 which is in agreement with Peng et al.<sup>14</sup> The  $\text{CeO}_2-\text{Sm}_2\text{O}_3$  sintered into dense ceramic. Fig. 9 shows the variation of density with composition. The density initially decreases and then increases with increase in  $\text{Sm}_2\text{O}_3$  content. Fig. 10 show the SEM images from  $0.5\text{CeO}_2-0.5\text{Sm}_2\text{O}_3$  ceramic, indicating a single phase nature. The SEM photographs show dense ceramic with grain size up to  $10 \mu\text{m}$  that are smaller in size as com-

pared to pure ceria. The XRD patterns recorded from samples with  $x > 0.5$  are in agreement with the monoclinic symmetry  $\text{Sm}_2\text{O}_3$ . The  $\text{Sm}_2\text{O}_3$  sintered up to 99% of the theoretical density ( $7.746 \text{ g cm}^{-3}$ ). The sintered  $\text{Sm}_2\text{O}_3$  has  $\epsilon_r = 23$ ,  $\tau_r = +22 \text{ ppm/}^\circ\text{C}$  and  $Q \times f = 46,000 \text{ GHz}$ . However the sintered samples decomposed and

became powder on aging. Addition of 0.5 wt.% of CuO prevented the decomposition problem.

Fig. 11 shows the Raman spectra of Sm-doped CeO<sub>2</sub> for compositions were  $X < 0.5$ . The linewidth (FWHM) of the 465 cm<sup>-1</sup> mode increases up to  $X = 0.2$  (from 10.5 to 37.3 cm<sup>-1</sup>) and thereafter decreases to 27.3 cm<sup>-1</sup> at  $X = 0.5$ . The same mode, which can be viewed as an indication of the Ce-O8 vibrations, shifts first to lower frequency when  $X$  goes to 0.1 (from 465.5 to 463.5 cm<sup>-1</sup>) before shifting higher to 473.1 cm<sup>-1</sup> at  $X = 0.3$  and finally lower again to 469.5 cm<sup>-1</sup> at  $X = 0.5$ . These shifts are due to the change of oxygen vacancies and valency changes which are introduced into the CeO<sub>2</sub> lattice when Sm<sup>3+</sup> substitute the Ce<sup>4+</sup>. Additional modes appear with more samarium addition where most noticeable are a couple of soft modes at 554 and 589 cm<sup>-1</sup>. The theory of changes of oxygen vacancies, which in return causes intrinsic losses, are supported by comparing the dielectric loss at low temperatures where a small addition of Sm ( $X = 0.01$ ) decreases the loss of pure CeO<sub>2</sub> at 100 K and by further addition of Sm, up

to  $X = 0.5$ , a steady decrease of the loss appear at the same temperature.

The maximum solubility of samarium into the lattice is about  $X = 0.5$ .<sup>14</sup> This can be observed in a drastic change of both  $\epsilon_r$  and  $Q$  at  $X = 0.5$  as shown in Fig. 12. The similar ionic size between Ce<sup>4+</sup> and Sm<sup>3+</sup> contribute to a much higher solubility than the CaTiO<sub>3</sub> doped composites. The variation of  $\epsilon_r$  and  $Q \times f$  of the (1-x)CeO<sub>2</sub>-xSm<sub>2</sub>O<sub>3</sub> as a function of  $x$  are shown in Fig. 12. The  $\epsilon_r$  of both Sm<sub>2</sub>O<sub>3</sub> and CeO<sub>2</sub> are nearly the same and so it is expected that  $\epsilon_r$  of the system remains almost the same through out the region under study. However there is a decrease in the  $\epsilon_r$  in the region  $0.01 \leq x \leq 0.50$ , which can be attributed to the decrease in relative density. The  $Q \times f$  increases from 70,000 to 90,000 GHz as  $x$  varies from zero to 0.5 and further increase in  $x$  decreases the quality factor. The  $\tau_f$  increases from -53 ppm/°C with increase in  $x$  and becomes positive value as shown in Fig. 13. The  $\tau_f$  becomes zero for  $x = 0.92$ .

Fig. 14 shows the variation of the quality factor on cooling the ceramic samples down to 20 K. In the case of CeO<sub>2</sub> the quality factor increases rapidly on cooling. The percentage increase in the quality factor on cooling

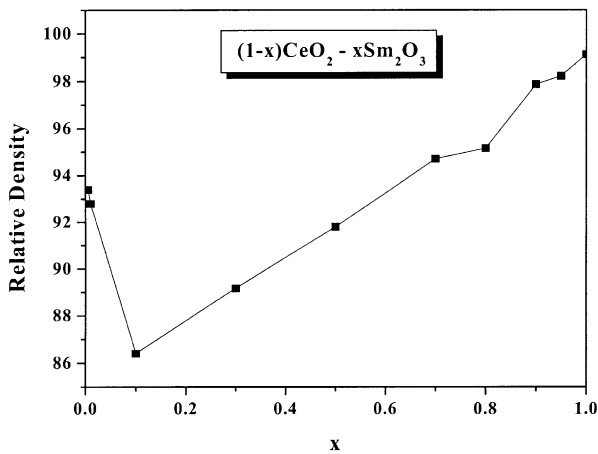


Fig. 9. Variation of the relative density of (1-x)CeO<sub>2</sub>-xSm<sub>2</sub>O<sub>3</sub> ceramics as a function of composition  $x$ .

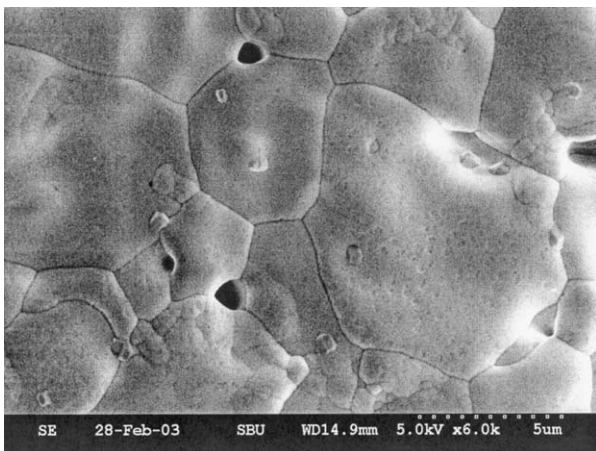


Fig. 10. Scanning electron micrograph of 0.5CeO<sub>2</sub>-0.5Sm<sub>2</sub>O<sub>3</sub> ceramic.

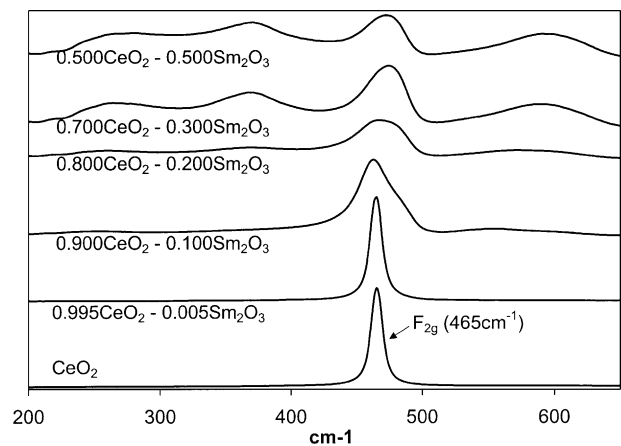


Fig. 11. Raman spectra of (1-x)CeO<sub>2</sub>-xSm<sub>2</sub>O<sub>3</sub> ceramics for different values of  $x$ .

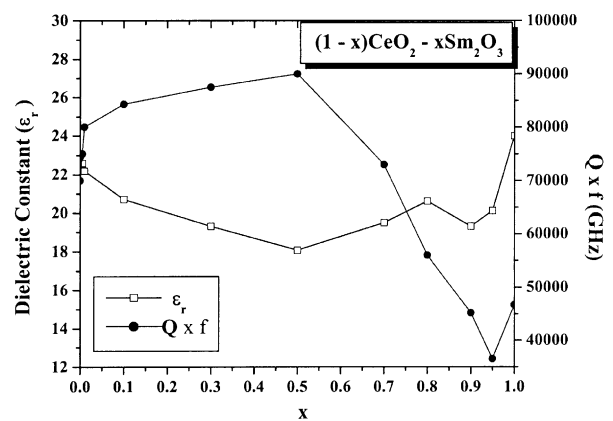


Fig. 12. Variation of  $\epsilon_r$  and  $Q \times f$  GHz of (1-x)CeO<sub>2</sub>-xSm<sub>2</sub>O<sub>3</sub> ceramics as a function of composition  $x$ .

decreases with increase in  $\text{Sm}_2\text{O}_3$  content. For 50 mol%  $\text{Sm}_2\text{O}_3$  addition, there is hardly any increase in the  $Q$  value on cooling. The  $0.5\text{CeO}_2-0.5\text{Sm}_2\text{O}_3$  has the highest  $Q$  at room temperature. The quality factor–temperature plot shows a dip or lowering of  $Q$  at about 100 K.

In order to study the effect of various rare earth ions with different ionic radii on the microwave dielectric properties of ceria 1 mol% each of rare oxide such as  $\text{Nd}_2\text{O}_3$ ,  $\text{Eu}_2\text{O}_3$ ,  $\text{Gd}_2\text{O}_3$  and  $\text{Er}_2\text{O}_3$  was added to calcined  $\text{CeO}_2$  and pellets were prepared. The microwave dielectric properties of these rare earth doped ceria are tabulated in Table 1. Table 1 shows that microwave

dielectric properties of ceria does not depend on the radii of the rare earth dopant ion.

#### 4. Conclusions

The  $(1-x)\text{CeO}_2-x\text{CaTiO}_3$  ( $0.1 \leq x \leq 0$ ) and  $(1-x)\text{CeO}_2-\text{Sm}_2\text{O}_3$  ( $0 \leq x \leq 1$ ) dielectric ceramics have been prepared by conventional solid state ceramic route. X-ray diffraction, SEM and Raman studies indicate that  $\text{CeO}_2-\text{CaTiO}_3$  form a solid solution phase. The  $\epsilon_r$  increases,  $Q$  decreases and  $\tau_f$  increases with  $\text{CaTiO}_3$  addition. The  $\epsilon_r$  of ceria increases with the addition of  $\text{CaTiO}_3$ , but decreases with  $\text{Sm}_2\text{O}_3$  addition. Complete temperature stability is achieved by the addition of 5.7 mol% of  $\text{CaTiO}_3$  to  $\text{CeO}_2$ . In the case of  $(1-x)\text{CeO}_2-x\text{Sm}_2\text{O}_3$  the  $Q$  increases up to about  $x=0.5$  beyond which the  $Q$  decreases and temperature compensation occurs at  $x=0.92$ . The microwave dielectric properties

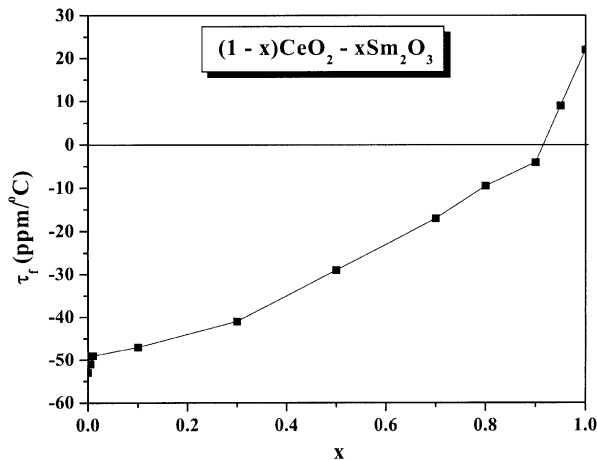


Fig. 13. Temperature coefficient of resonant frequency ( $\tau_f$ ) of  $(1-x)\text{CeO}_2-\text{Sm}_2\text{O}_3$  ceramics as a function of composition  $x$ .

Table 1

Microwave dielectric properties of 1 mol% rare earth (RE) doped ceria

RE	$Q \times f$ (GHz)	$\epsilon_r$	$\tau_f$ (ppm/K)
Nd	51,000	22.80	-63
Sm	90,000	23.93	-50
Eu	30,000	24.00	-78
Gd	48,000	24.20	-55
Er	74,000	23.50	-60

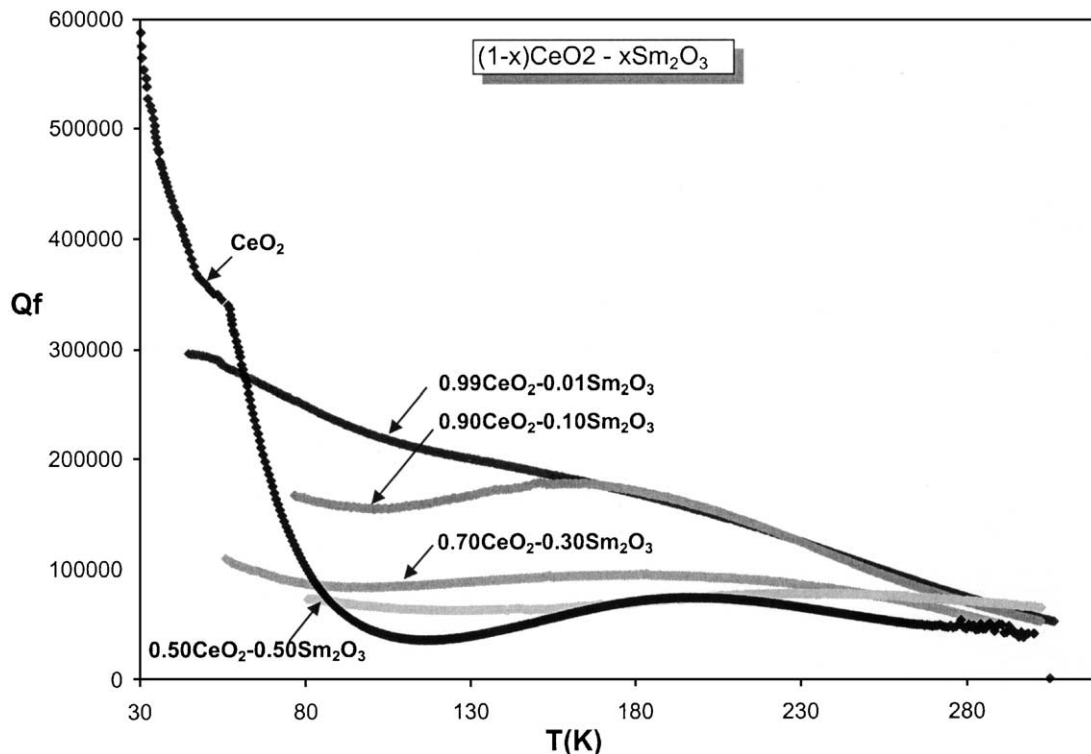


Fig. 14. Variation of quality factor ( $Q \times f$  GHz) as a function of temperature on cooling.

of ceria are not depended on the ionic radius of the dopant rare earth ions. SEM studies show that addition of  $\text{Sm}_2\text{O}_3$  and  $\text{CaTiO}_3$  reduces the grain size of the  $\text{CeO}_2$  ceramics.

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